Chemistry 240 Semester 01-2009 Homework for Submission #2

Answer the following question and submit them for marking on or before Thursday 5th February in class. If any answers show evidence of copying, the whole exercise will attract zero marks. Please note that presentation of your answer (not neatness as such!) is extremely important.

1) Radon is a radioactive noble gas. It is produced in granitic rocks by the radioactive decay of uranium. It has a short half-life, but apart from that would not be expected to present a significant threat at altitude. Demonstrate the truth of this statement by applying the barometric formula to show that if the gas is expelled at sea level the number of radon atoms at 100 m is expected to be considerably diminished. Take the temperature as 27° C. (Hint: calculate N₁/N₀.)

2) Jean Perrin, a Frenchman (shown on the right), was awarded the Noble prize in 1922. In 1909 he conducted a beautiful series of experiments on sedimentation equilibria. These are governed by the Boltzmann distribution as shown below:

$$\frac{N_1}{N_0} = e^{-mg(h_1 - h_0)/kt}$$

He examined a suspension of fine gamboge particles of radius 0.212 µm in water. These have a density of 1.207×10^{-3} kg m³ as compared with that of water of 1.00×10^{3} kg m⁻³. This gives each of the particles an effective mass of $\frac{4}{3}\pi r^{3}(\rho_{g} - \rho_{w})$ where ρ_{g} represents the density of the gamboge and ρ_{w} the density of the water.

Derive the expression

$$\ln(N) = \frac{-4\pi r^3 (\rho_g - \rho_w)gh}{3kT} + \ln(N_0)$$

for the relative numbers of gamboge particles at height h (N) as compared with the number at height $h_0 = 0$ (N₀) from the Boltzmann distribution.

Height h / µm	5	35	65	95
N (relative units)	100	47	22.6	12

The following data are taken from one of Perrin's experiments:

Plot ln(N) against h and from the slope of the straight-line graph determine k. Given that $R = 8.31 \text{ JK}^{-1} \text{mol}^{-1}$, $g = 9.81 \text{ ms}^{-2}$ and $T = 20^{\circ}\text{C}$, calculate L (Avogadro's number). (This was an early experiment, and only gives a rather rough estimate of L.)

